

Area Theorems

[Proof and Use]

16.1 INTRODUCTION

Area of a plane figure is the region bounded by it.

Students have already used formulae for finding the areas of different geometrical figures. For example :

area of a triangle = $\frac{1}{2}$ base \times height

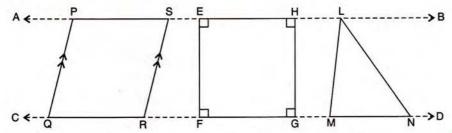
area of a rectangle = length × breadth

area of a parallelogram = base x height and so on.

In the current chapter, we shall be *comparing* the areas of different geometrical figures, such as parallelograms, rectangles and triangles subject to certain conditions.

- 1. Equal figures mean, the figures equal in area.
- 2. Congruent figures are always equal in area, but the converse is not always true.

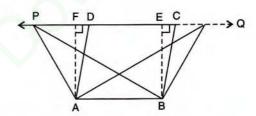
16.2 FIGURES BETWEEN THE SAME PARALLELS



If a parallelogram PQRS, a rectangle EFGH and a triangle LMN are so drawn that their bases lie on the same straight line (say, CD) and their other vertices lie on another straight line (say, AB) parallel to CD, then the parallelogram PQRS, the rectangle EFGH and the triangle LMN are said to be between the same parallels.

It is obvious that the parallelogram, the rectangle and the triangle between the same parallels have equal altitudes (height).

- Note: 1. In the figure, given above, if QR = FG = MN, we say that the figures PQRS, EFGH and LMN are on equal bases and between the same parallels.
 - 2. In the figure, given alongside, if PQ is parallel to AB, then the figures PAB, FABE, DABC, QAB, etc. are said to be on the same base and between the same parallels.

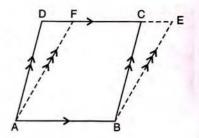


Theorem 19

Parallelograms on the same base and between the same parallels are equal in area.

Given: Parallelograms ABCD and ABEF are on the same base AB and between the same parallels AB and DE.

To Prove: Area of (//gm ABCD) = Area of (//gm ABEF). Proof:



Statement:

Reason:

In \triangle ADF and \triangle BCE.

- 1. AD = BC[Opposite sides of //gm ABCD]
- 2. $\angle ADF = \angle BCE$ [Corresponding angles] 3.
- [Corresponding angles] $\angle AFD = \angle BEC$ $\angle DAF = \angle CBE$.. [Since, two angles of both the Δs are equal;
 - therefore their third angle will also be equal] $\triangle ADF \cong \triangle BCE$ [A.S.A.]
 - Area (\triangle ADF) = Area (\triangle BCE) [Congruent Δs are equal in area]
 - \Rightarrow Area (Δ ADF) + Area (ABCF) [Adding, area (ABCF) on both the sides] = Area (\triangle BCE) + Area (ABCF)
 - ⇒ Area (//gm ABCD) = Area (//gm ABEF)

Hence proved.

Corollary:

Since, rectangle is a parallelogram also, the above theorem can also be stated as:

"The area of a parallelogram is equal to the area of a rectangle on the same base and between the same parallels."

Theorem 20

The area of a triangle is half that of a parallelogram on the same base and between the same parallels.

Given: Triangle ABC and parallelogram ABDE on the same base AB and between the same parallels AB and ED.

To Prove: Area (\triangle ABC) = $\frac{1}{2}$ Area (//gm ABDE)

Construction: Complete the parallelogram ABFC.

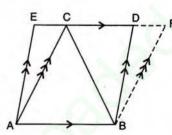


Statement:

Reason:

- 1. Since, BC is the diagonal of //gm ABFC.
 - ∴ Area (\triangle ABC) = $\frac{1}{2}$ Area (//gm ABFC)
- [Diagonal divides a //gm into two equal triangles]
- 2. Area (//gm ABFC) = Area (//gm ABDE) [//gms on the same base and between the same parallels are equal in area]
 - ∴ Area (\triangle ABC) = $\frac{1}{2}$ Area (//gm ABDE) [From statements 1 and 2]

Hence Proved.



Theorem 21

Triangles on the same base and between the same parallels are equal in area.

Given: \triangle ABC and \triangle ABD are on the same base AB and between the same parallels AB and CD.

To Prove: Area (\triangle ABC) = Area (\triangle ABD).

Construction: Complete the //gms ABEC and ABFD.

Proof:

Statement:

BC is diagonal of //gm ABEC,

∴ Area (\triangle ABC) = $\frac{1}{2}$ Area (//gm ABEC)

[Diagonal bisects the //gm]

Reason:

2. BD is diagonal of //gm ABFD,

∴ Area (\triangle ABD) = $\frac{1}{2}$ Area (//gm ABFD)

[Diagonal bisects the //gm]

3. Area (//gm ABEC) = Area (//gm ABFD)

: Area (Δ ABC) = Area (Δ ABD)

[//gms on the same base and between the same parallels are equal in area]
[From statements 1, 2 and 3]

AADD)

Hence Proved.

Corollaries:

1. Parallelograms on equal bases and between the same parallels are equal in area.

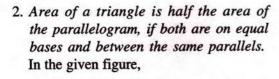
From the given figure,

Area (//gm ABCD) = Area (//gm EFGH).

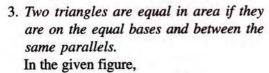
Similarly, if ABCD is a parallelogram and EFGH is a rectangle on equal bases and between the same parallels, then also

Area (//gm ABCD)

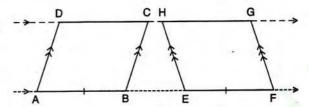
= Area (rect. EFGH).

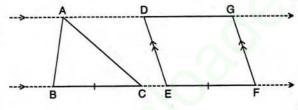


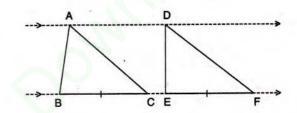
Area (\triangle ABC) = $\frac{1}{2}$ Area (//gm DEFG)



Area (\triangle ABC) = Area (\triangle DEF)



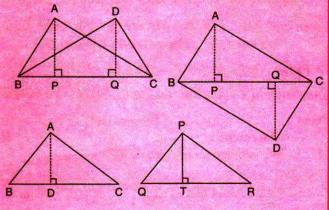




If two triangles have equal area and stand on the same base (or, equal bases) then their corresponding altitudes are engal.

In each of the given figures, Δ ABC and Δ DBC are on the same base (BC) and have equal areas, then their corresponding altitudes are equal, i.e., AP = DQ.

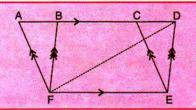
Similarly, if base BC of Δ ABC is equal to base QR of Δ PQR and their areas are also equal, then the corresponding altitudes AD and PT of these two triangles are also equal i.e. AD = PT





In the adjoining figure, area of parallelogram AFEC is 140 cm². State, giving reason, the area of:

- (i) parallelogram BFED.
- (ii) triangle BFD.



Solution:

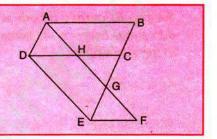
- (i) Parallelograms BFED and AFEC are on the same base FE and between the same parallels AD // FE, so they are equal in area.
- ∴ Ar. (parallelogram BFED) = Ar. (parallelogram AFEC) = 140 cm²

Ans.

(ii) Δ BFD and parallelogram BFED are on the same base BD and between the same parallels BD // FE, so area of the triangle BFD is half the area of parallelogram BFED.

.. Ar. (
$$\triangle$$
 BFD) = $\frac{1}{2}$ × Ar. (parallelogram BFED)
= $\frac{1}{2}$ × 140 cm² = 70 cm² Ans.

2 In the given figure, AB // DC // EF, AD // BE and DE // AF. Prove that the area of parallelogram DEFH is equal to the area of parallelogram ABCD.



Solution:

Parallelogram DEFH and parallelogram DEGA are on the same base DE and between the same parallels DE // AF, so they are equal in area.

i.e. Area of DEFH = Area of DEGA I

Parallelogram ABCD and parallelogram DEGA are on the same base AD and between the same parallels AD // BE; so they are equal in area.

From I and II, Area of DEFH = Area of ABCD

Hence proved.



P is any point inside a parallelogram ABCD. Prove that:

Area (
$$\triangle$$
 APB) + Area (\triangle CPD)
= Area (\triangle APD) + Area (\triangle BPC)

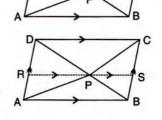
Solution:

The adjoining figure shows a parallelogram ABCD. Point P is inside ABCD and PA, PB, PC and PD are joined.

Through point P, draw RS parallel to AB which meets AD at R and BC at S.

Since, \triangle APB and parallelogram ARSB are on the same base AB and between the same parallels *i.e.* AB // RS.

∴ Area (
$$\triangle$$
 APB) = $\frac{1}{2}$ × Area (// gm ARSB) I



Similarly, Δ CPD and parallelogram DRSC are on the same base DC and between the same parallels DC // RS.

:. Area (
$$\triangle$$
 CPD) = $\frac{1}{2}$ × Area (// gm DRSC) II

Adding I and II, we get: Area (\triangle APB) + Area (\triangle CPD)

=
$$\frac{1}{2}$$
 × Area (// gm ARSB) + $\frac{1}{2}$ × Area (// gm DRSC)

$$= \frac{1}{2} [Area (// gm ARSB) + Area (// gm DRSC)]$$

=
$$\frac{1}{2}$$
 × Area (// gm ABCD) III

Now, draw MN through point P such that MN // AD and cuts AB at N and CD at M.

Since Δ APD and parallelogram ANMD are on the same base AD and between the same parallels (AD // MN).

$$\therefore \qquad \text{Area } (\Delta \text{ APD}) = \frac{1}{2} \times \text{Area } (// \text{ gm ANMD})$$

Similarly, Δ BPC and parallelogram BNMC are on the same base BC and between the same parallels (BC // MN).

$$\therefore \qquad \text{Area } (\Delta \text{ BPC}) = \frac{1}{2} \times \text{Area } (// \text{ gm BNMC})$$

Adding, Area (
$$\triangle$$
 APD) + Area (\triangle BPC)

=
$$\frac{1}{2}$$
 × Area (// gm ABCD) IV

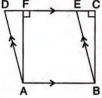
From equations III and IV, we get:

Area (\triangle APB) + Area (\triangle CPD) = Area (\triangle APD) + Area (\triangle BPC)

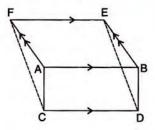
Hence proved.

EXERCISE 16(A)

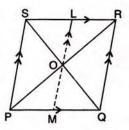
- 1. In the given figure, if area of triangle ADE is 60 cm²; state, giving reason, the area of:
 - (i) parallelogram ABED; D F E C
 - (ii) rectangle ABCF;
 - (iii) triangle ABE.



- 2. The given figure shows a rectangle ABDC and a parallelogram ABEF; drawn on opposite sides of AB. Prove that:
 - (i) quadrilateral CDEF is a parallelogram;
 - (ii) Area of quad. CDEF
 - = Area of rect. ABDC
 - + Area of //gm. ABEF.



3. In the given figure, diagonals PR and QS of the parallelogram PQRS intersect at point O and LM is parallel to PS. Show that:



- (i) 2 Area (\triangle POS) = Area (//gm PMLS)
- (ii) Area (\triangle POS) + Area (\triangle QOR)

=
$$\frac{1}{2}$$
 Area (//gm PQRS)

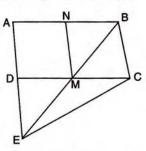
(iii) Area (\triangle POS) + Area (\triangle QOR) =Area (\triangle POQ) + Area (\triangle SOR). 4. In parallelogram ABCD, P is a point on side AB and Q is a point on side BC.

Prove that:

- (i) Δ CPD and Δ AQD are equal in area.
- (ii) Area (Δ AQD)

= Area (
$$\triangle$$
 APD) + Area (\triangle CPB)

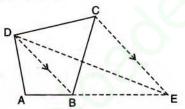
5. In the given figure, A M and N are the mid-points of the sides DC and AB respectively of the parallelogram ABCD.



If the area of parallelogram ABCD is 48 cm²;

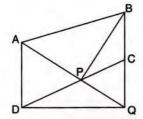
- (i) state the area of the triangle BEC.
- (ii) name the parallelogram which is equal in area to the triangle BEC.
- 6. In the following figure, CE is drawn parallel to diagonal DB of the quadrilateral ABCD which meets AB produced at point E.

Prove that Δ ADE and quadrilateral ABCD are equal in area.



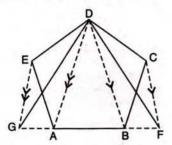
 $\triangle ADE = \triangle ADB + \triangle BDE$ $= \triangle ADB + \triangle BDC$ = Ouad. ABCD

ABCD is a parallelogram, a line through A cuts DC at point P and BC produced at Q.
 Prove that triangle BCP is equal in area to triangle DPQ.

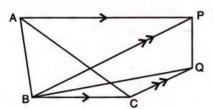


 The given figure shows a pentagon ABCDE.
 EG drawn parallel to DA meets BA produced at G and CF drawn parallel to DB meets AB produced at F.

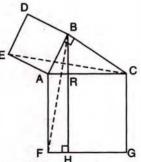
Prove that the area of pentagon ABCDE is equal to the area of triangle GDF.



In the given figure, AP is parallel to BC, BP is parallel to CQ. Prove that the areas of triangles ABC and BQP are equal.



10. In the figure given alongside, squares ABDE and AFGC are drawn on the side AB and the E hypotenuse AC of the right triangle ABC.

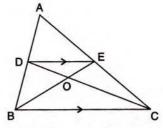


If BH is perpendicular to FG, prove that:

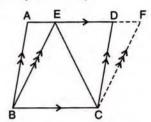
- (i) $\Delta EAC \cong \Delta BAF$.
- (ii) Area of the square ABDE

= Area of the rectangle ARHF.

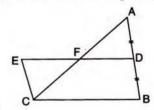
- 11. In the following figure, DE is parallel to BC. Show that:
 - (i) Area (\triangle ADC) = Area (\triangle AEB)
 - (ii) Area (\triangle BOD) = Area (\triangle COE).



12. ABCD and BCFE are parallelograms. If area of triangle EBC = 480 cm², AB = 30 cm and BC = 40 cm; Calculate;



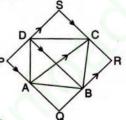
- (i) area of parallelogram ABCD;
- (ii) area of the parallelogram BCFE;
- (iii) length of altitude from A on CD;
- (iv) area of triangle ECF.
- 13. In the given figure, D is mid-point of side AB of ΔABC and BDEC is a parallelogram.



Prove that:

Area of \triangle ABC = Area of // gm BDEC.

14. In the following figure, AC // PS // QR and PO // DB // SR.



Prove that:

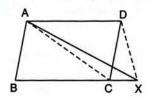
Area of quadrilateral PQRS = $2 \times$ Area of quad. ABCD.

15. ABCD is a trapezium with AB // DC. A line parallel to AC intersects AB at point M and BC at point N. Prove that : area of Δ ADM = area of Δ ACN.

Join C and M

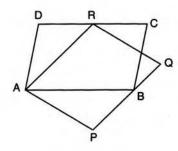
AD // BE // CF.
Prove that :
area (ΔAEC)
= area (ΔDBF)

 In the given figure, ABCD is a parallelogram BC is produced to point X. Prove that:
 area (Δ ABX) = area (quad. ACXD)



and APQR. Show that these parallelograms are equal in area.

[Join B and R]



4 Prove that a median divides a triangle into two triangles of equal area.

Solution :

Given: A ABC with AD as median.

To prove: Area (\triangle ABD) = Area (\triangle ADC) = $\frac{1}{2}$ Area (\triangle ABC)

Construction: Draw AP \perp BC.

Proof: Since, area of a $\Delta = \frac{1}{2}$ base \times height (altitude)

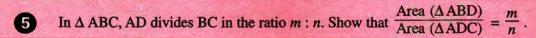
$$\therefore \quad \text{Area } (\Delta \text{ ABD}) = \frac{1}{2} \text{ BD} \times \text{AP}$$

and, Area (
$$\triangle$$
 ADC) = $\frac{1}{2}$ DC \times AP.

$$= \frac{1}{2} BD \times AP \quad [\because DC = BD]$$

∴ Area (
$$\triangle$$
 ABD) = Area (\triangle ADC) = $\frac{1}{2}$ Area (\triangle ABC)

Hence Proved.

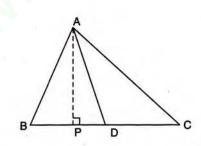


Solution:

Given; AD divides BC in the ratio m:n, therefore, $\frac{BD}{DC} = \frac{m}{n}$

To Prove: $\frac{\text{Area}(\Delta \text{ ABD})}{\text{Area}(\Delta \text{ ADC})} = \frac{m}{n}$

Construction: Draw AP ⊥ BC.



Proof: Since, Area (\triangle ABD) = $\frac{1}{2}$ BD \times AP

and, Area (\triangle ADC) = $\frac{1}{2}$ DC × AP

$$\therefore \frac{\text{Area } (\triangle \text{ ABD})}{\text{Area } (\triangle \text{ ADC})} = \frac{\frac{1}{2} \text{ BD} \times \text{AP}}{\frac{1}{2} \text{ DC} \times \text{AP}} = \frac{\text{BD}}{\text{DC}} = \frac{m}{n}$$

$$\left(\text{Given } : \frac{\text{BD}}{\text{DC}} = \frac{m}{n}\right)$$

Hence Proved.

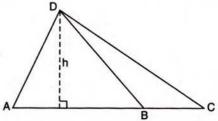
16.3 TRIANGLES WITH THE SAME VERTEX AND BASES ALONG THE SAME LINE

The given figure shows Δ ABD, Δ BCD and Δ ACD with the same vertex D and bases along the same straight line AC, so they have the same height. In such a case, the areas of triangles are in the ratio of their bases.

$$\therefore (i) \frac{\text{Area of } \triangle ABD}{\text{Area of } \triangle BCD} = \frac{AB}{BC}$$

(ii)
$$\frac{\text{Area of } \Delta \text{ABD}}{\text{Area of } \Delta \text{ACD}} = \frac{\text{AB}}{\text{AC}}$$
 and

(iii)
$$\frac{\text{Area of } \Delta BCD}{\text{Area of } \Delta ACD} = \frac{BC}{AC}$$



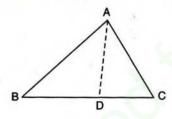
6 In triangle ABC, D is a point in side BC such that 2BD = 3DC. Prove that the area of triangle ABD = $\frac{3}{5}$ × Area of \triangle ABC.

Solution :

$$2BD = 3DC$$

$$\Rightarrow \frac{BD}{DC} = \frac{3}{2}$$

$$\Rightarrow \frac{BD}{BD + DC} = \frac{3}{3 + 2} \Rightarrow \frac{BD}{BC} = \frac{3}{5}$$



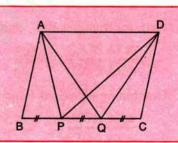
Since, \triangle ABD and \triangle ABC have the same vertex A and their bases along the same straight line BC, the areas of the triangles are in the ratio of their bases.

$$\therefore \frac{\text{Ar.}(\Delta \text{ ABD})}{\text{Ar.}(\Delta \text{ ABC})} = \frac{\text{BD}}{\text{BC}} \Rightarrow \frac{\text{Ar.}(\Delta \text{ ABD})}{\text{Ar.}(\Delta \text{ ABC})} = \frac{3}{5} \Rightarrow \text{Ar.}(\Delta \text{ ABD}) = \frac{3}{5} \times \text{Ar.}(\Delta \text{ ABC})$$

Hence proved.

In parallelogram ABCD, points P and Q lie on side BC and trisect it. Prove that :
ar.(Δ APQ) = ar.(Δ DPQ)

$$= \frac{1}{6} \times \text{ ar. (parallelogram ABCD)}$$



Solution:

Given:
$$BP = PQ = QC$$

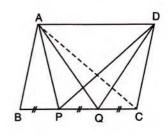
⇒ Bases of triangles ABP and ABC are in the ratio 1:3

i.e.
$$BP : BC = 1 : 3$$

and their vertices are at the same point (point A)

$$\therefore \frac{\text{ar.}(\Delta \text{ ABP})}{\text{ar.}(\Delta \text{ ABC})} = \frac{\text{BP}}{\text{BC}} = \frac{1}{3}$$

$$\Rightarrow$$
 ar(\triangle ABP) = $\frac{1}{3}$ × ar.(\triangle ABC)



In parallelogram ABCD, AC is diagonal so it bisects the parallelogram.

$$\Rightarrow \quad \text{ar.}(\Delta \text{ ABC}) = \frac{1}{2} \times \text{ar.}(//\text{gm ABCD}) \qquad \dots \text{II}$$

Equations I and II give:

$$ar.(\Delta ABP) = \frac{1}{3} \times \frac{1}{2} \times ar.(//gm ABCD)$$

$$\Rightarrow \quad \text{ar.}(\Delta \text{ ABP}) = \frac{1}{6} \times \text{ar.}(//\text{gm ABCD})$$

Since, Δ ABP, Δ APQ and Δ DPQ are on equal bases and between the same parallels; therefore:

$$ar.(\Delta ABP) = ar.(\Delta APQ) = ar.(\Delta DPQ)$$

....Ш

....I

$$\operatorname{ar.}(\Delta \text{ APQ}) = \operatorname{ar.}(\Delta \text{ DPQ}) = \frac{1}{6} \times \operatorname{ar.}(//\operatorname{gm} \text{ ABCD})$$

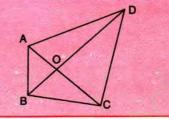
(From equations III and IV)

Hence proved.

8 In the given figure, ABCD is a quadrilateral with diagonals AC and BD intersecting at point O.

Prove that:

$$ar.(\Delta AOD) \times ar.(\Delta BOC) = ar.(\Delta AOB) \times ar.(\Delta COD)$$



Solution:

Whenever, the triangles have their bases along the same line and vertices at the same point, the ratio between their areas is equal to ratio between their bases.

:. For triangles AOB and AOD,

$$\frac{\operatorname{ar.}(\Delta \text{ AOB})}{\operatorname{ar.}(\Delta \text{ AOD})} = \frac{\operatorname{BO}}{\operatorname{DO}}$$

....I

And, for triangles BOC and COD,

$$\frac{\operatorname{ar.}(\Delta \operatorname{BOC})}{\operatorname{ar.}(\Delta \operatorname{COD})} = \frac{\operatorname{BO}}{\operatorname{DO}}$$

....П

Combining equations I and II, we get:

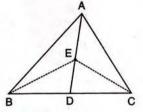
$$\frac{\operatorname{ar.}(\Delta \operatorname{AOB})}{\operatorname{ar.}(\Delta \operatorname{AOD})} = \frac{\operatorname{ar.}(\Delta \operatorname{BOC})}{\operatorname{ar.}(\Delta \operatorname{COD})}$$

$$\Rightarrow$$
 ar.(\triangle AOD) \times ar.(\triangle BOC) = ar.(\triangle AOB) \times ar.(\triangle COD)

Hence proved.

1. Show that:

- (i) a diagonal divides a parallelogram into two triangles of equal area.
- (ii) the ratio of the areas of two triangles of the same height is equal to the ratio of their bases.
- (iii) the ratio of the areas of two triangles on the same base is equal to the ratio of their heights.
- 2. In the given figure; AD is median of ΔABC and E is any point on median AD. Prove that Area (ΔABE) = Area (ΔACE).

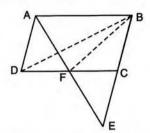


- 3. In the figure of question 2, if E is the mid point of median AD, then prove that : $Area (\Delta ABE) = \frac{1}{4} Area (\Delta ABC).$
- ABCD is a parallelogram. P and Q are the mid-points of sides AB and AD respectively.
 Prove that area of triangle APQ = ¹/₈ of the area of parallelogram ABCD.

Join PD and BD.

5. The base BC of triangle ABC is divided at D so that BD = $\frac{1}{2}$ DC. Prove that area of \triangle ABD = $\frac{1}{3}$ of the area of \triangle ABC.

- In a parallelogram ABCD, point P lies in DC such that DP: PC = 3: 2. If area of Δ DPB = 30 sq. cm, find the area of the parallelogram ABCD.
- ABCD is a parallelogram in which BC is produced to E such that CE = BC and AE intersects CD at F.

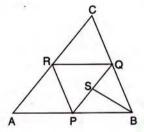


If $ar.(\Delta DFB) = 30 cm^2$; find the area of parallelgoram

By A.S.A. \triangle ADF \cong \triangle ECF \Rightarrow DF = CF and so BF is median of \triangle BDC.

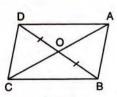
8. The following figure shows a triangle ABC in which P, Q and R are mid-points of sides AB, BC and CA respectively. S is mid-point of PO.

Prove that : $ar.(\Delta ABC) = 8 \times ar.(\Delta QSB)$



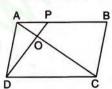
EXERCISE 16(C)

 In the given figure, the diagonals AC and BD intersect at point O. If OB = OD and AB//DC, prove that:



- (i) Area (\triangle DOC) = Area (\triangle AOB).
- (ii) Area (\triangle DCB) = Area (\triangle ACB).
- (iii) ABCD is a parallelogram.

The given figure shows a parallelogram ABCD with area 324 sq. cm. P is a point in AB such that AP: PB = 1: 2. Find:



- (i) the area of Δ APD.
- (ii) the ratio OP: OD.

 In Δ ABC, E and F are mid-points of sides AB and AC respectively. If BF and CE intersect each other at point O, prove that the Δ OBC and quadrilateral AEOF are equal in area.

First of all prove that:

Ar. of \triangle BOE = Ar. of \triangle COF

Now, BF is a median

 $\Rightarrow \Delta ABF = \Delta CBF$

 $\Rightarrow \Delta ABF - \Delta BOE = \Delta CBF - \Delta COF$

- In parallelogram ABCD, P is mid-point of AB. CP and BD intersect each other at point O. If area of Δ POB = 40 cm², find:
 - (i) OP: OC
 - (ii) Areas of Δ BOC and Δ PBC
 - (iii) Areas of Δ ABC and parallelogram ABCD.
- 5. The medians of a triangle ABC intersect each other at point G. If one of its medians is AD, prove that:
 - (i) Area (\triangle ABD) = 3 × Area (\triangle BGD)
 - (ii) Area (\triangle ACD) = 3 × Area (CGD)
 - (iii) Area (\triangle BGC) = $\frac{1}{3}$ × Area (\triangle ABC)
- 6. The perimeter of a triangle ABC is 37 cm and the ratio between the lengths of its altitudes be 6:5:4. Find the lengths of its sides.

Let the sides be x cm, y cm and (37 - x - y) cm. Also, let the lengths of altitudes be 6a cm, 5a cm and 4a cm

 \therefore Area of a triangle = $\frac{1}{2} \times \text{base} \times \text{altitude}$

$$\therefore \frac{1}{2} \times x \times 6a = \frac{1}{2} \times y \times 5a = \frac{1}{2} (37 - x - y) \times 4a$$

 $\Rightarrow 6x = 5y = 148 - 4x - 4y$

 $\Rightarrow 6x = 5y \qquad \text{and} \quad 6x = 148 - 4x - 4y$

 $\Rightarrow 6x - 5y = 0$ and 10x + 4y = 148

7. In the given figure, E is mid-point of AB and DE meets diagonal AC at point F. If ABCD

is a parallelogram and area of Δ ADF is 60 cm²; find :

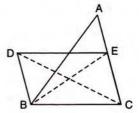
- (i) DF: FE
- (ii) area of Δ ADE
- (iii) area of Δ ADB
- (iv) area of // gm ABCD

$$AE = \frac{1}{2} AB = \frac{1}{2} DC$$

Δ DFC ~ Δ EFA

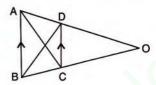
$$\Rightarrow \frac{DF}{FE} = \frac{DC}{AE} = \frac{DC}{\frac{1}{2}DC} = \frac{2}{1}$$

8. In the following figure, BD is parallel to CA, E is mid-point of CA and BD = $\frac{1}{2}$ CA.



Prove that : $ar.(\Delta ABC) = 2 \times ar.(\Delta DBC)$

In the following figure, OAB is a triangle and AB//DC.



If the area of Δ CAD = 140 cm² and the area of Δ ODC = 172 cm², find

- (i) the area of \triangle DBC
- (ii) the area of Δ OAC
- (iii) the area of Δ ODB.